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**Advatech Pacific**

**Changing The Way Engineering Is Conducted™**



# Analysis of Coaxial Injectors Using CFD++

Presenter:

Henry Vu, Ph.D.

*This material is based upon work supported by  
AFRL/RZSA, AFRL/RZSE, and AFRL/RZST under Contract Nos.  
FA9300-06-D-0002 and FA9300-10-C-4002*



# Overview

- Company Background
- Current CFD projects
- Coaxial Jet Flow with Variable Density
- Coaxial Particle Laden Flow



# Advatech Pacific, Inc. Background



- An Aerospace Engineering Research & Development Company Founded in 1995 primarily focused on:
  - Aerospace Vehicle Physics-based Modeling, Simulation and Analysis
  - Electronic Communications System Interoperability
  - Aerospace Engineering Design and Analysis Services



# Contract Objectives

- Objectives

- Modeling and analysis of fluid flows and heat transfer in support of experiments performed at AFRL Edwards
  - Complement experimental data by providing detailed visualization of fluid flow and thermal distributions inside experiments
  - Supplement experimental data by generating data at test conditions not performed in experiments
- Provide independent verification and validation for CFD++ code development



# Contract Objectives



## ● CFD Projects

- Coaxial Particle laden flow dynamics to assist in design of an experimental apparatus
- Coaxial gas/gas injector flow analysis for rocket fuel injector design
- Mixing of jet in cross-flow for pre-burner studies
- Evaluation of pipe flow conditioning devices
- Conjugate heat transfer studies in pipe flow for experimental design.



# COAXIAL JET FLOW WITH VARIABLE DENSITY

Collaborators: S. Alexander Schumaker, Ananda Himansu,  
Stephen Danczyk, Malissa Lightfoot



# Motivation

- Liquid propellant rocket engine injectors characterized by low velocity, high density inner jet and high velocity, low density annular jet.
- Conservation equations linked through density variations.
- Need to determine accuracy of RANS predictions in flows with large density differences.
- Validate Metacomp CFD++ tool for relevant flows.

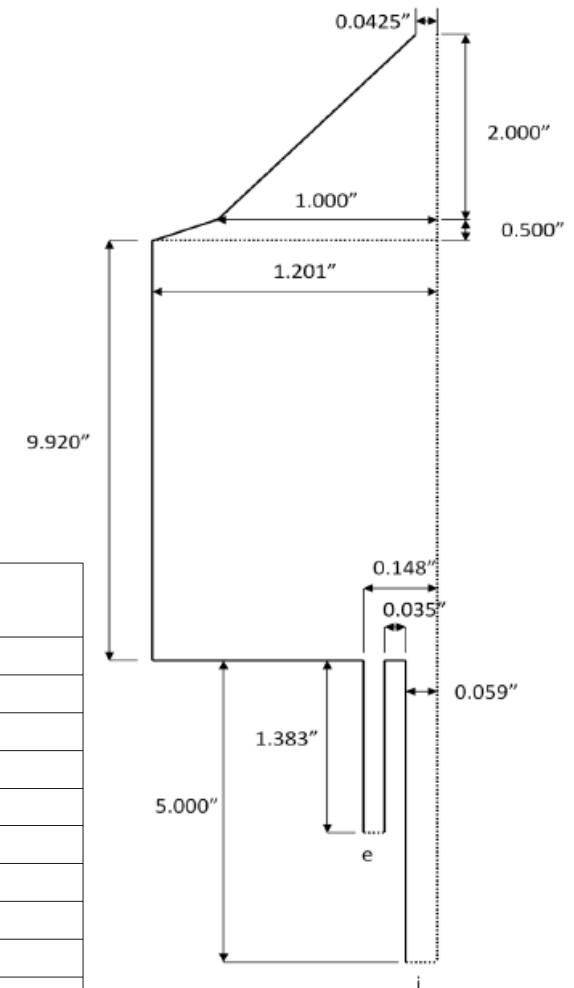




# Michigan SEI Case

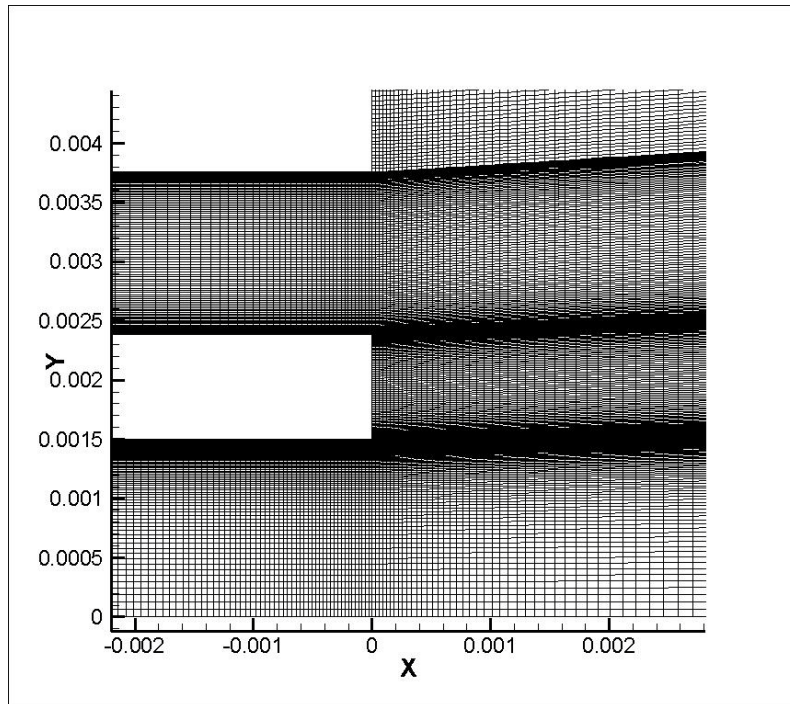
- PLIF concentration data for single element injector
- Low speed flow for ease of modeling
- Confined flow with nozzle at the exit
- Inner fluid (i) is air seeded with acetone
- Outer fluid (e) is helium
- $\rho_i/\rho_e=7.5$

Inner Fluid (i)	Air with 3.35% Acetone by Volume	
Molecular Weight (i)	29.95	Kg/kmol
Molecular Weight (e)	4.003	Kg/kmol
Chamber Pressure	543829.7	Pa
To (e)	293	K
To (i)	293	k
$\rho_o$ (e)	0.894	Kg/m <sup>3</sup>
$\rho_o$ (i)	6.685	Kg/m <sup>3</sup>
Uavg (e) in tube	63.559	m/s
Uavg (i) in tube	12.587	m/s
Mdot (e)	1.50136E-3	Kg/s
Mdot (i)	5.93253E-4	Kg/s

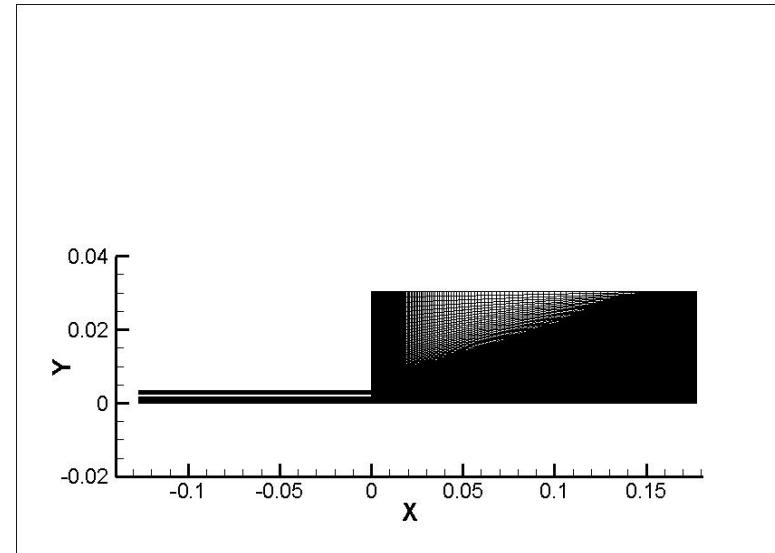




# Michigan SEI Case



Mesh:  
2D axisymmetric  
93386 quadrilateral cells,  $y+=1$



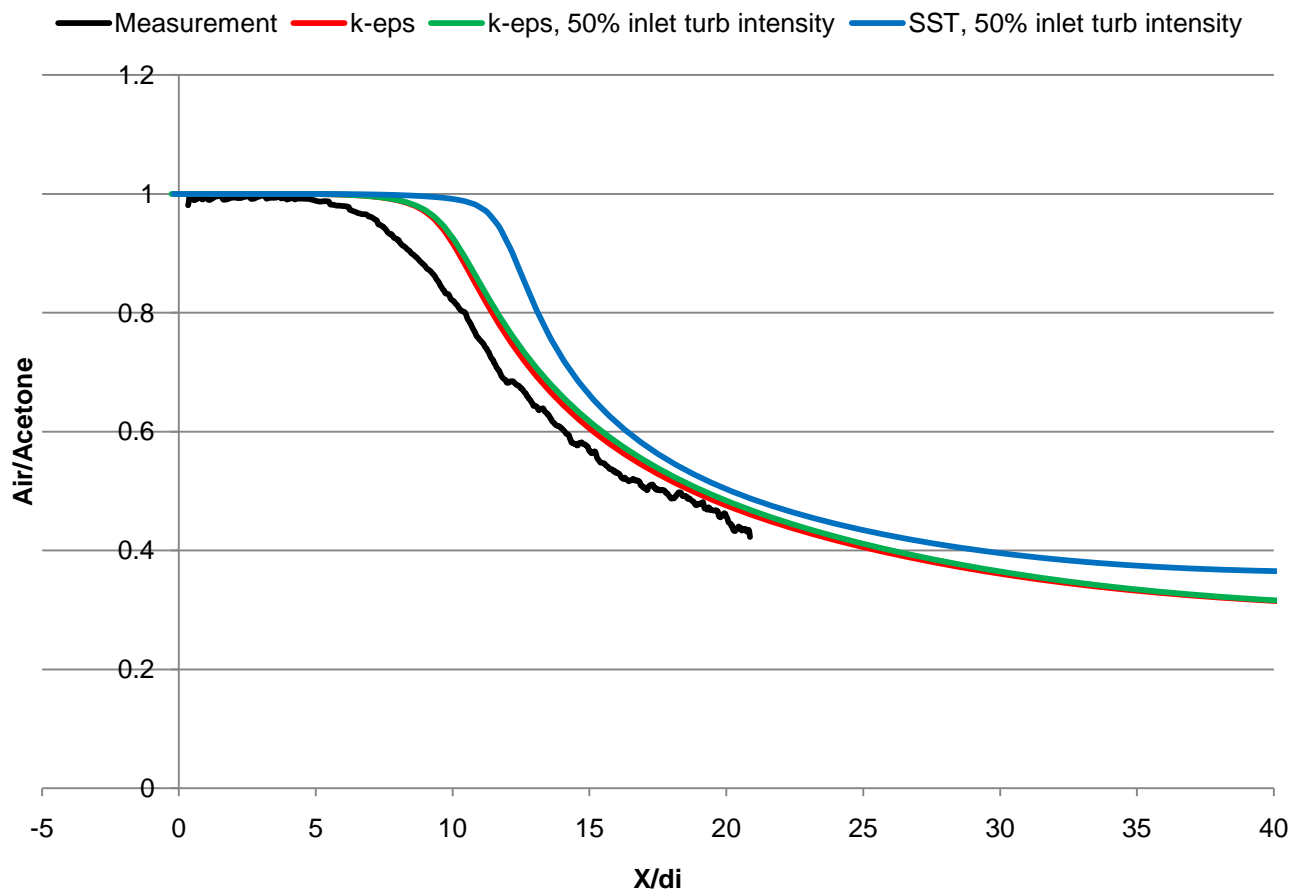
## Case Conditions:

- Two species (He, Air/Acetone)
- Base Equation Type: Compressible Real Gas Navier-Stokes/Euler
- Equation of State: Ideal Gas
- Turbulence Simulation: RANS, realizable k-eps or SST
- Turbulence Intensity: 2% or 50%
- nozzle geometry at the exit remove and replaced with back pressure imposition



# Michigan SEI Case

## Centerline Mass Fraction

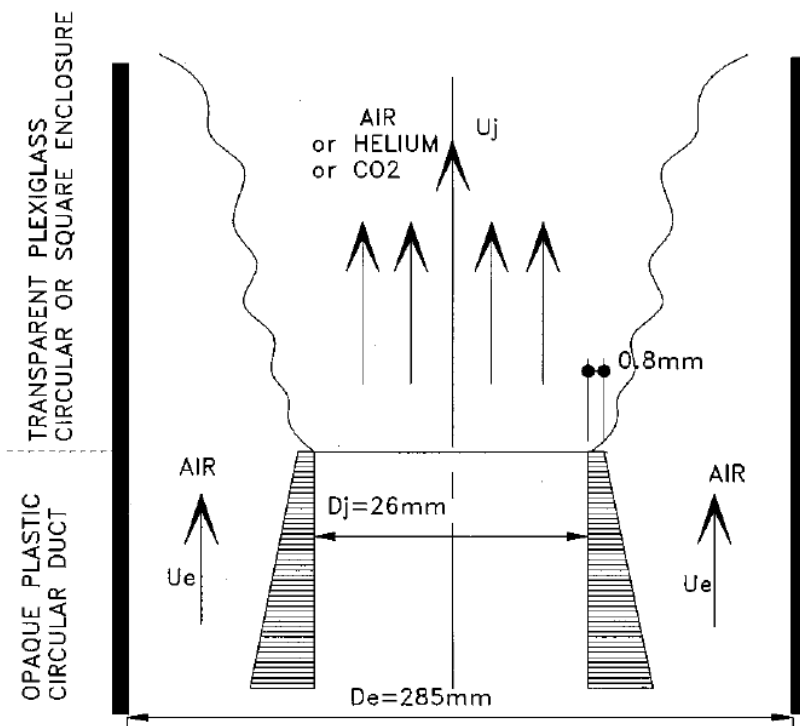


- At least 15% error in concentration along the centerline in the near-field
- No improvement by increase turbulence at inlet
- SST turbulence model makes result worse

***Is error due to problem in modeling scalar or velocity field?***



# Validation Case



- 2D axisymmetric compressible RANS
- Density-based solver
- Realizable k-eps turbulence solved to the wall
- $T=300$  K and  $P=101325$  Pa
- Center inlet boundary:
  - He normal velocity = 24.45 m/s
  - Air normal velocity = 10.5 m/s
  - $\text{CO}_2$  normal velocity = 9.0 m/s
- Outer inlet boundary: Air with normal velocity of 0.9 m/s
- Outlet: Simple back pressure outlet of 0 Pa.

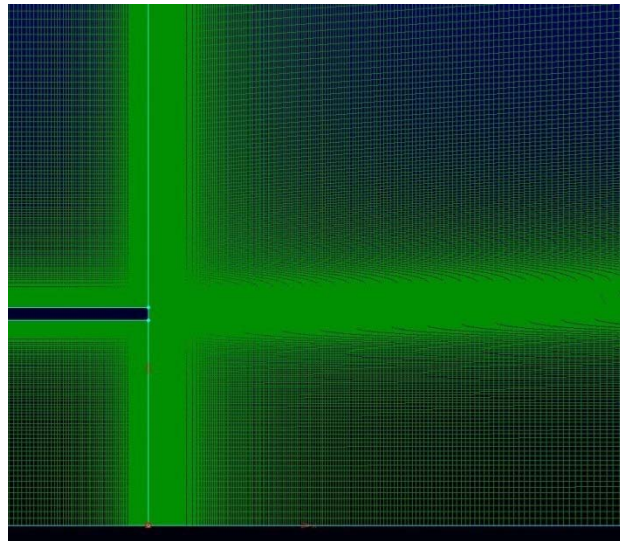
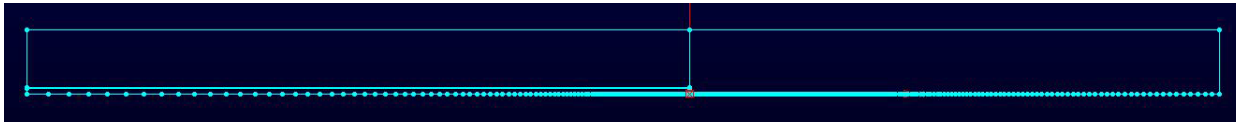
Gas	$U_j$ [m/s] (Expt)	$U_j$ [m/s] (CFD)	$Re_j$	$\rho_j/\rho_e$
He	32	31.4	7000	0.14
Air	12	12.68	21000	1
$\text{CO}_2$	10	10.75	32000	1.4

Amielh, M., Djeridane, T., Anselmet, F., & Fulachier, L. (1996). Velocity near-field of variable density turbulent jets. *Int. J. Heat Mass Transfer*, 2149-2164.

Djeridane, T., Amielh, M., Anselmet, F., & Fulachier, L. (1996). Velocity turbulence properties in the near-field region of axisymmetric variable density jets. *Phys. Fluids*, 1614-1630.



# Validation Case

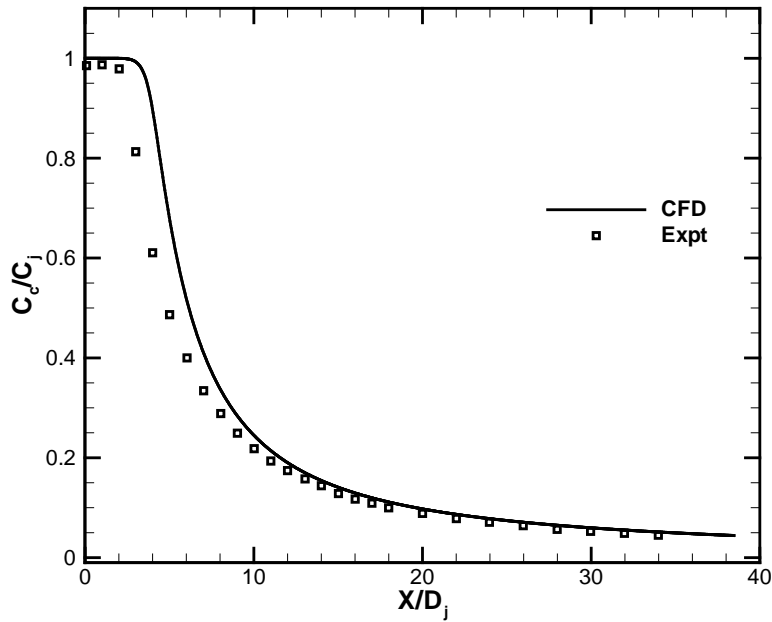


- 234880 quadrilateral cells with a  $y^+$  of 1 or less at all wall locations except the outermost wall.
- Run up length = 1.5 m
- Total domain length = 2.7 m



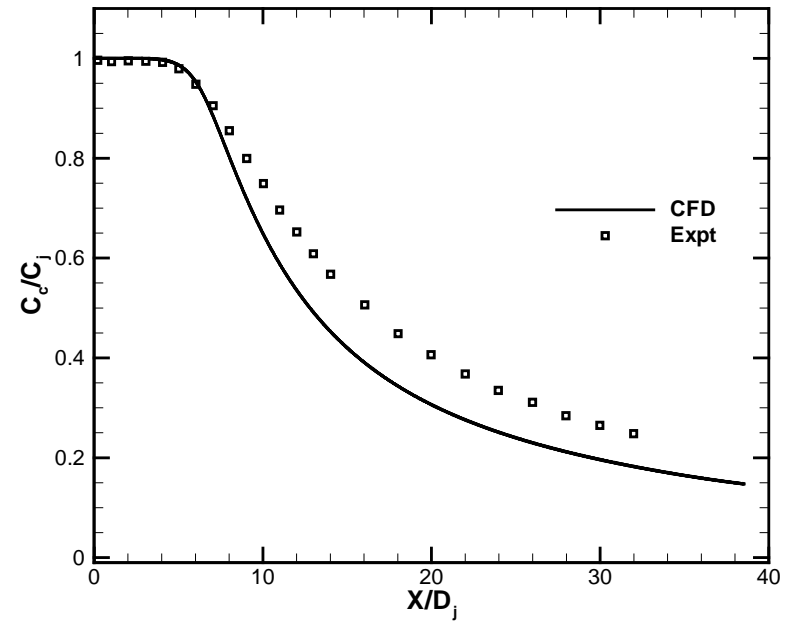
# Validation Case Results

Mean Streamwise Mass Fraction



He

Mean Streamwise Mass Fraction

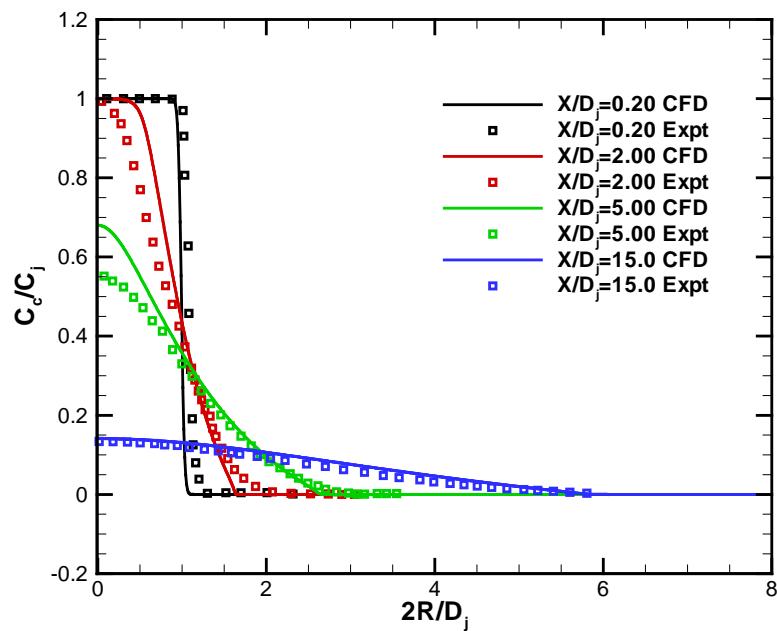


$CO_2$



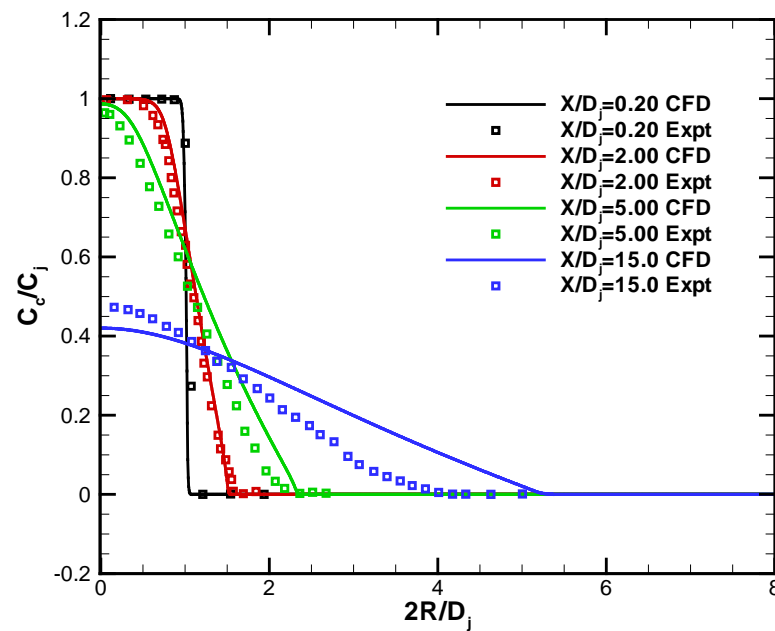
# Validation Case Results

Radial Profiles of Mean Mass Fraction



He

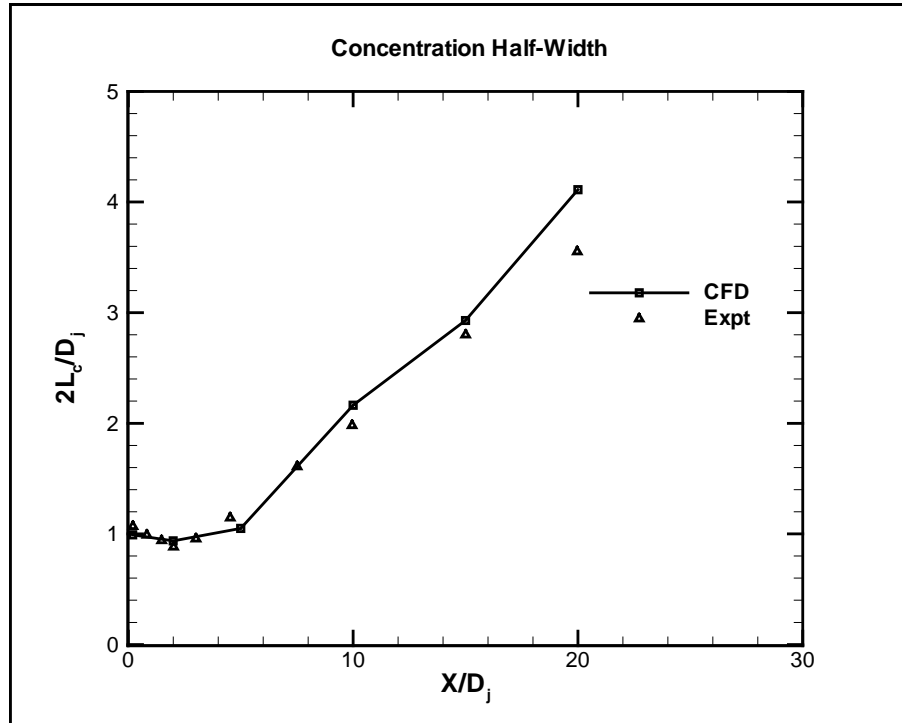
Radial Profiles of Mean Mass Fraction



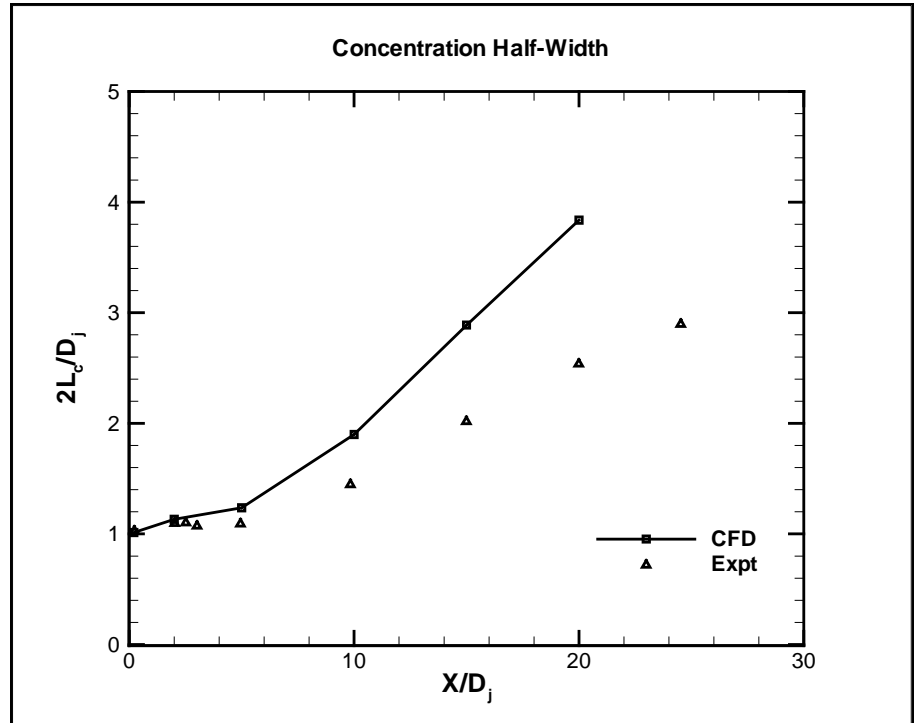
$CO_2$



# Validation Case Results



He

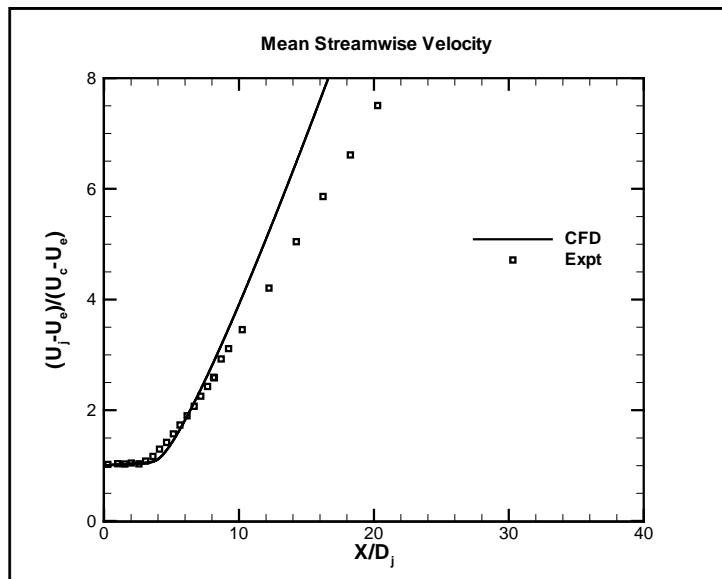


CO<sub>2</sub>

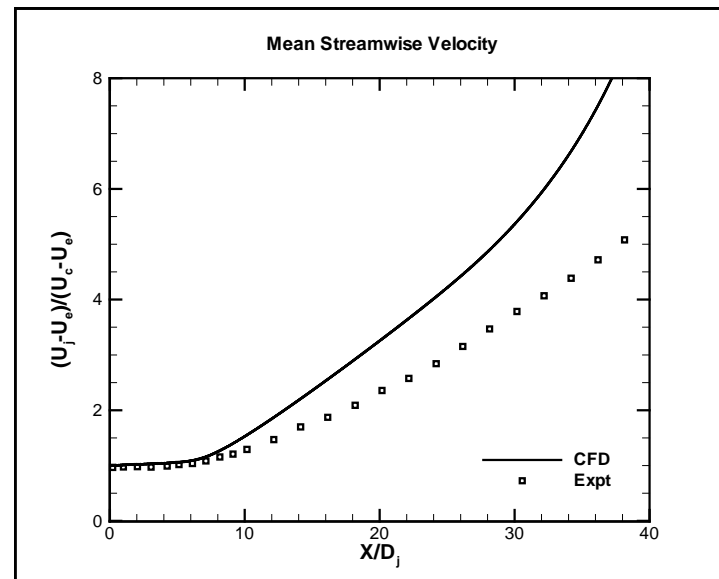




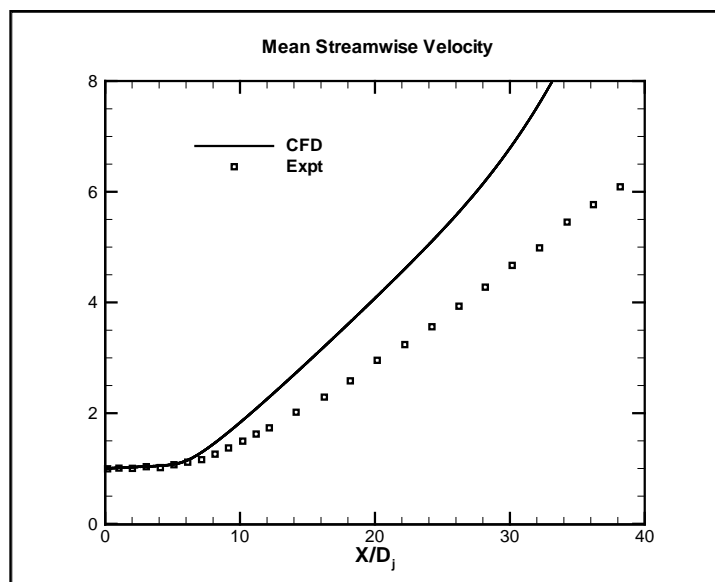
# Validation Case Results



He



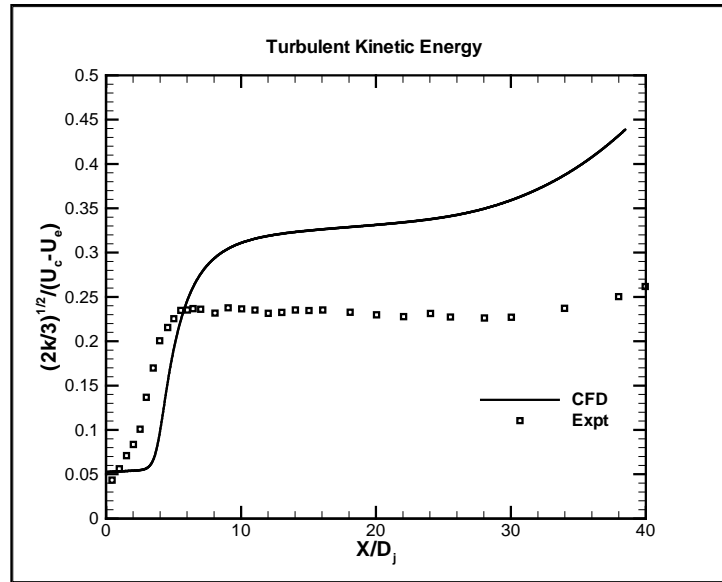
CO<sub>2</sub>



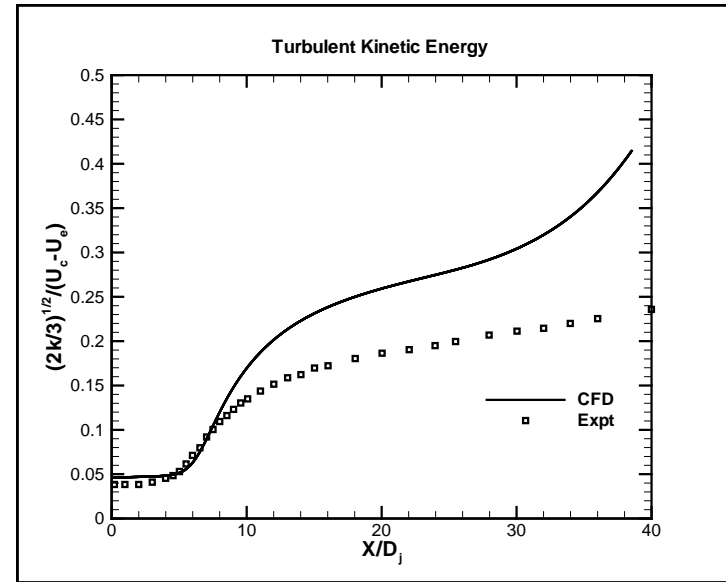
Air



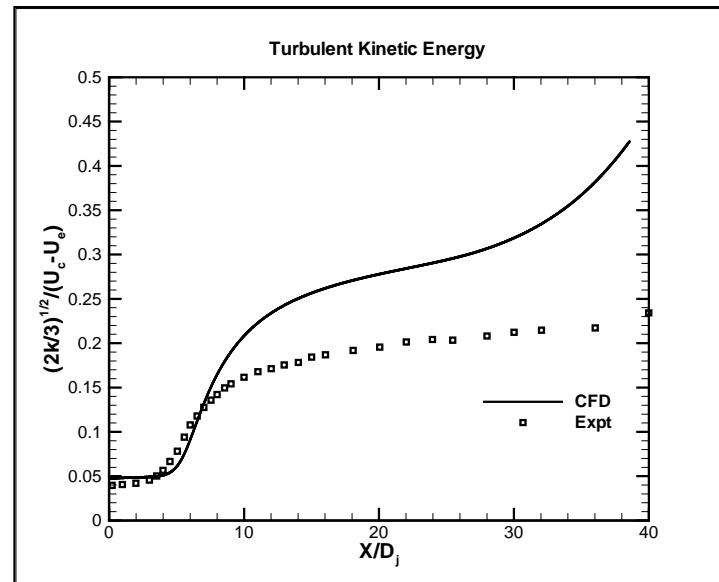
# Validation Case Results



He



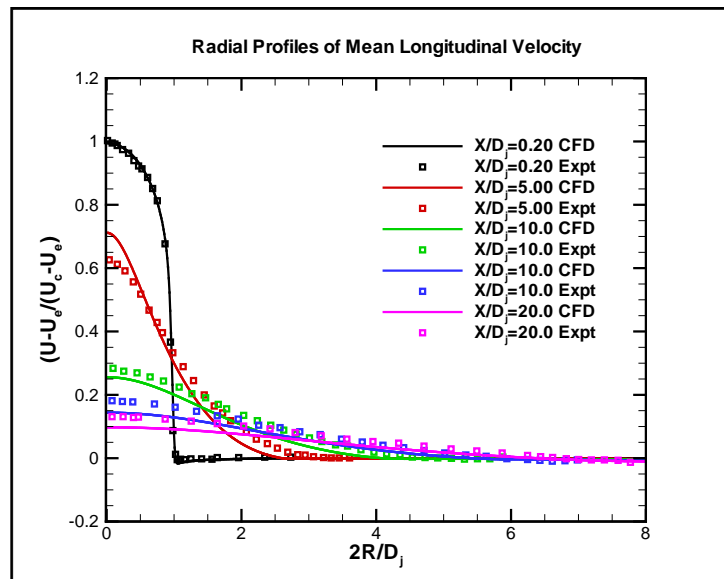
CO<sub>2</sub>



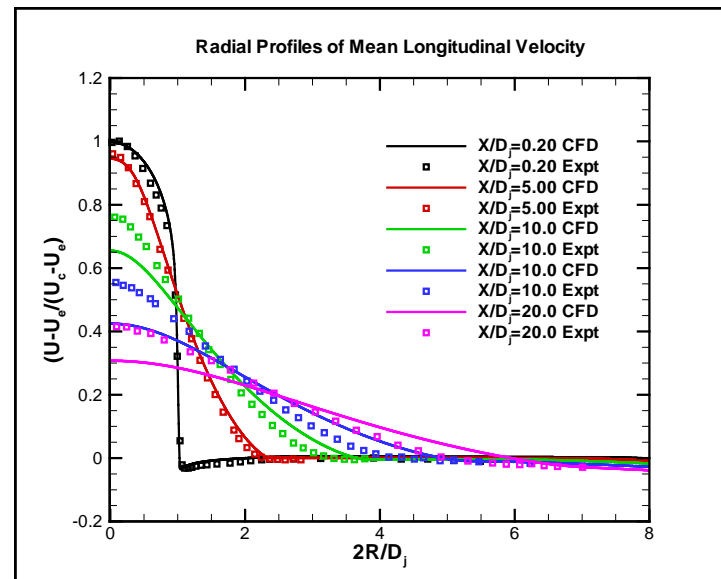
Air



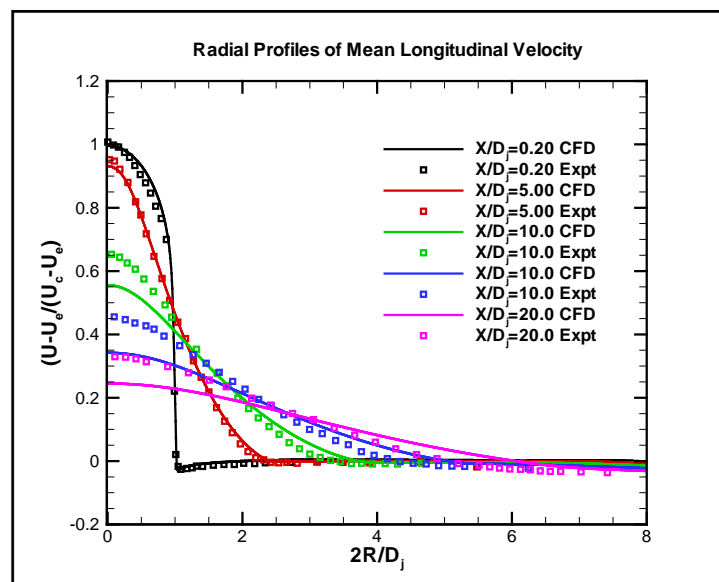
# Validation Case Results



He



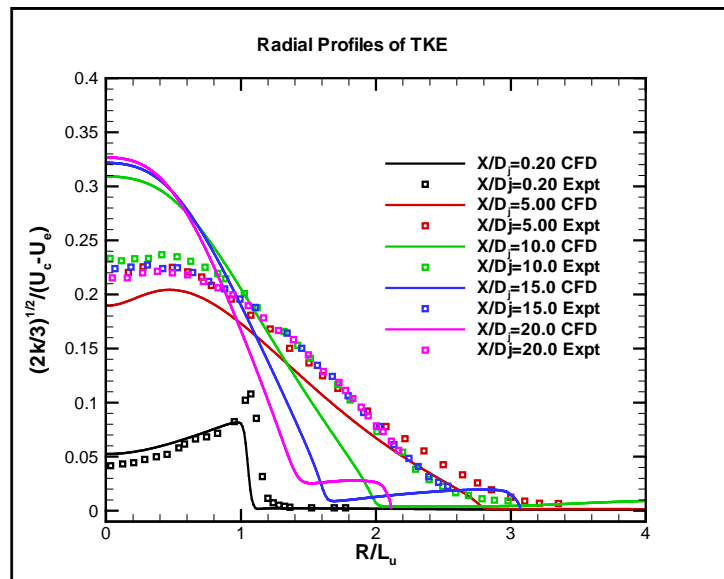
CO<sub>2</sub>



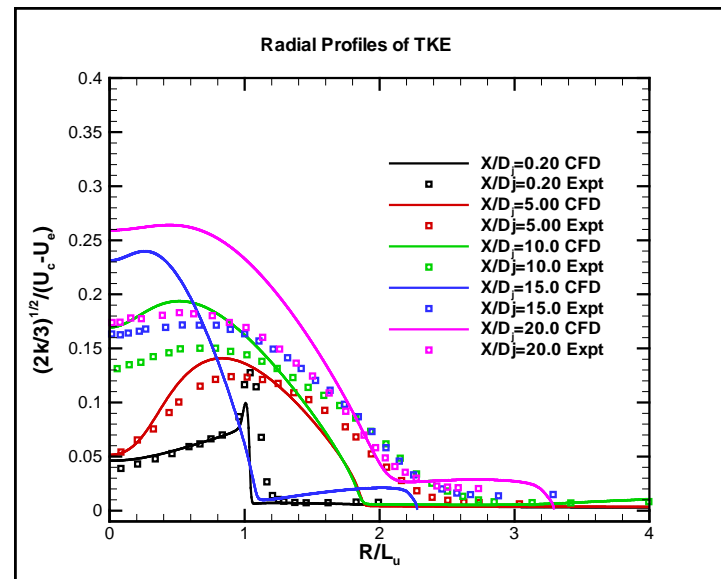
Air



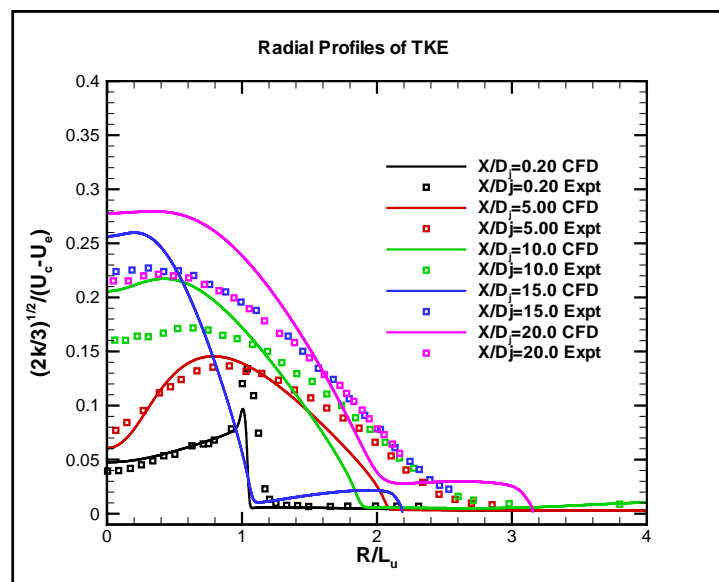
# Validation Case Results



He



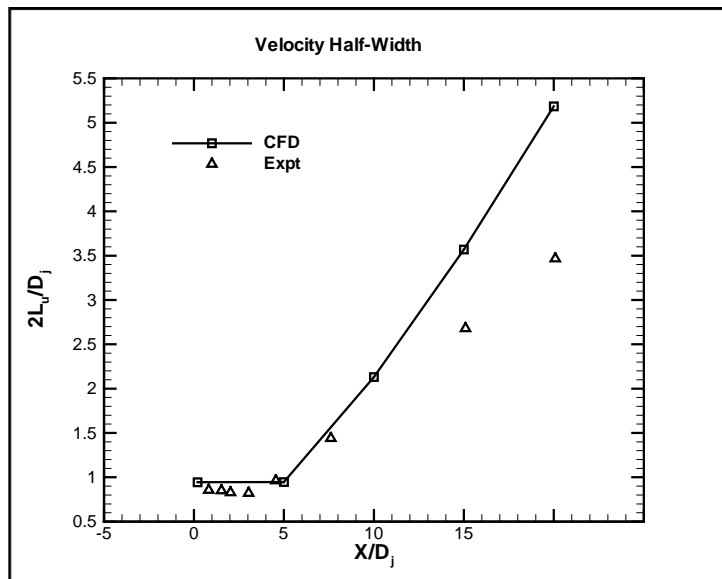
CO<sub>2</sub>



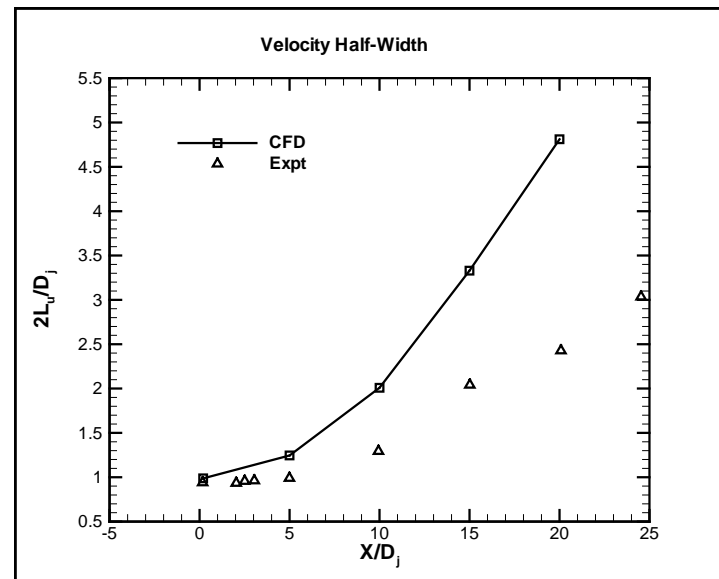
Air



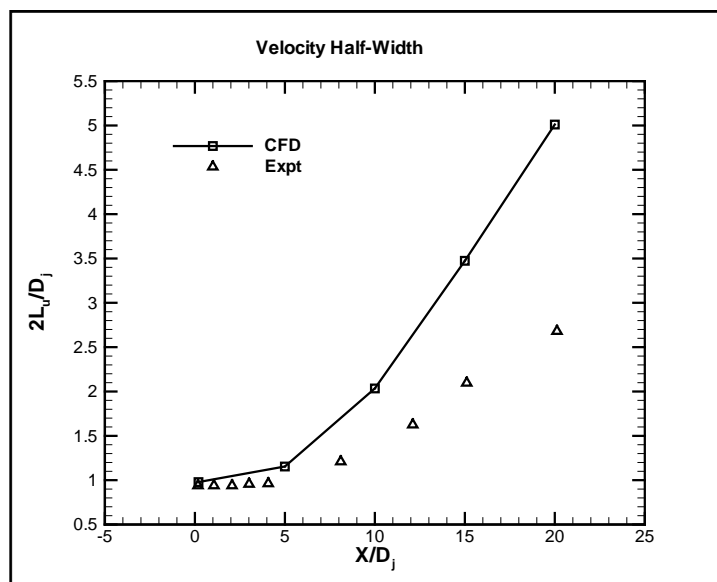
# Validation Case Results



He



CO<sub>2</sub>



Air



# Validation Case Summary

- Case exhibits same deficiency in centerline mixing for He/Air in the near field while improving in the far-field.
- Radial profiles of mean quantities generally good, except at centerline.
- CO<sub>2</sub>/Air case shows accurate mixing in the near-field and worsens downstream.
- Both CFD and experiment show low sensitivity of density ratio on jet spreading. Mixing occurring by entrainment of surrounding fluid.
- Turbulence is generally over predicted everywhere except in the near field for He/Air.
- Deficiencies in centerline mixing may be correlated to turbulence.



# Future Work

- Try difference turbulence models.
- Modify k-eps to compensate for low near-field turbulence.
- Try Large Eddy Simulation (LES).
- Proceed to more relevant flow conditions for rocket injectors.



# COAXIAL PARTICLE LADEN FLOW

Collaborators: Ananda Himansu, Alireza Badakhshan, Stephen Danczyk





# Motivation

- Experimental set up in lab to evaluate novel fuel ignition strategies
- USI device with a shroud to induce swirl in coflow
- Use CFD to help design apparatus and flow conditions
- Some earlier CFD work helped in redesign of shroud for better swirling
- A parametric study to test the effects of swirling flow showed some unusual results
- Need to validate dispersed phase modeling features in CFD++ to confirm results and determine important conditions to accurate modeling



# Eulerian Dispersed Phase Modeling in CFD++



## Dispersed Phase

Mass: 
$$\frac{\partial(\rho_{pi})}{\partial t} + \nabla \cdot (\rho_{pi} \vec{u}_{pi}) = \dot{m}_i$$

Momentum: 
$$\frac{\partial(\rho_{pi} \vec{u}_{pi})}{\partial t} + \nabla \cdot (\rho_{pi} \vec{u}_{pi} \vec{u}_{pi}) = \vec{F}_{D_i} + \vec{F}_{V.M._i} + \vec{F}_{T.D._i} + \vec{F}_{L_i} + \vec{F}_{P.G._i} + \vec{F}_{B_i} + \dot{m}_i \vec{u}_{pi}$$

Energy: 
$$\begin{aligned} \frac{\partial(\rho_{pi} e_{pi}^0)}{\partial t} + \nabla \cdot (\rho_{pi} e_{pi}^0 \vec{u}_{pi}) &= \text{Conduction source term} + \text{Radiation source term} + \dot{m}_i e_{pi}^0 \\ &= \dot{Q}_{pi} + \dot{m}_i e_{pi}^0 \end{aligned}$$

Number Density: 
$$\frac{\partial N_i}{\partial t} + \nabla \cdot (N_i \vec{u}_{pi}) = 0$$

Melting Fraction: 
$$\frac{\partial(\xi_i N_i)}{\partial t} + \nabla \cdot (\xi_i N_i \vec{u}_{pi}) = \text{Melting source term}$$

Material Density: 
$$\tilde{\rho}_{pi} = \tilde{\rho}_{pi_{liquid}} \xi_i + \tilde{\rho}_{pi_{solid}} (1 - \xi_i),$$

Particle radius: 
$$r_i = \left( \frac{3\rho_{pi}}{4\pi\tilde{\rho}_{pi}N_i} \right)^{1/3}.$$



# Eulerian Dispersed Phase Modeling in CFD++



## Continuous Phase

Momentum source terms:

$$\sum_{i=1}^{NP} \left( \vec{F}_{D_i} + \vec{F}_{V.M.i} + \vec{F}_{T.D.i} \right) ,$$

Energy source terms:

$$\sum_{i=1}^{NP} \left[ \frac{\rho_{pi} C_{pi} f_{Ni}}{\tau_{Ti}} (T_f - T_{pi}) + \vec{u}_f \cdot (\vec{F}_{D_i} + \vec{F}_{V.M.i} + \vec{F}_{T.D.i}) \right] .$$

## Relevant Source Terms

Interphase Drag:

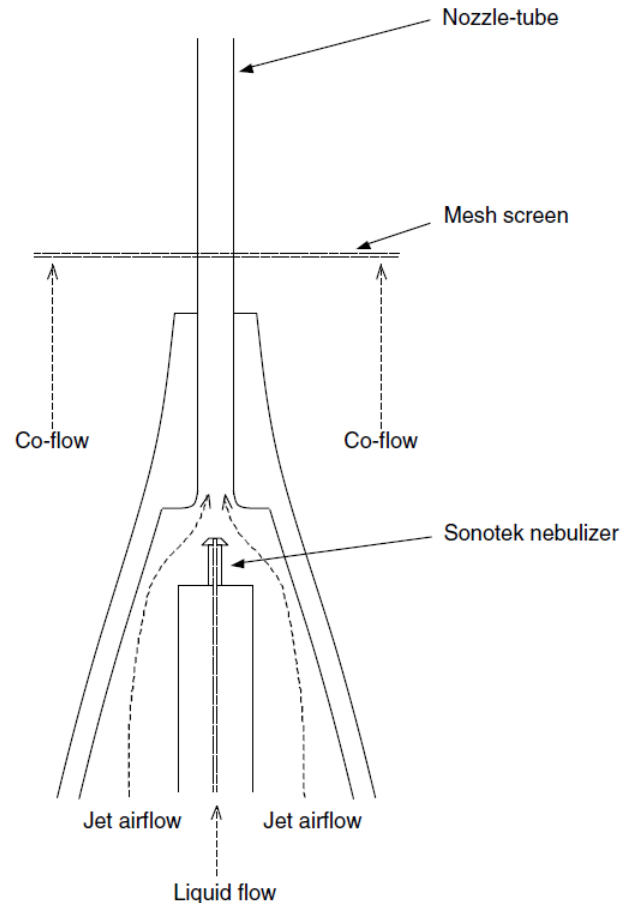
$$\frac{\vec{F}_{D_i}}{\rho_{pi}} = \frac{f_{Di}}{\tau_{ui}} (\vec{u}_f - \vec{u}_{pi}) ,$$

Turbulent Dispersion:

$$\frac{\vec{F}_{T.D.i}}{\rho_{pi}} = -\frac{f_{Di}}{\tau_{ui}} \frac{\nu_t}{Pr_t} \left( \frac{\nabla \eta_{pi}}{\eta_{pi}} - \frac{\nabla \eta_f}{\eta_f} \right) ,$$



# Model Validation Case



Poly-dispersed  
turpentine droplets

$$d = 1-90 \text{ } \mu\text{m}$$

$$U_c = 2.4 \text{ m/s}$$

Low turbulence  
intensity of 1.4%

Nijdam, J., Langrish, T., & Fletcher, D. (2008). Assessment of an Eulerian CFD model for prediction of dilute droplet dispersion in a turbulent jet. *Appl. Math. Model.*, 2686-2705.



# Model Validation Case

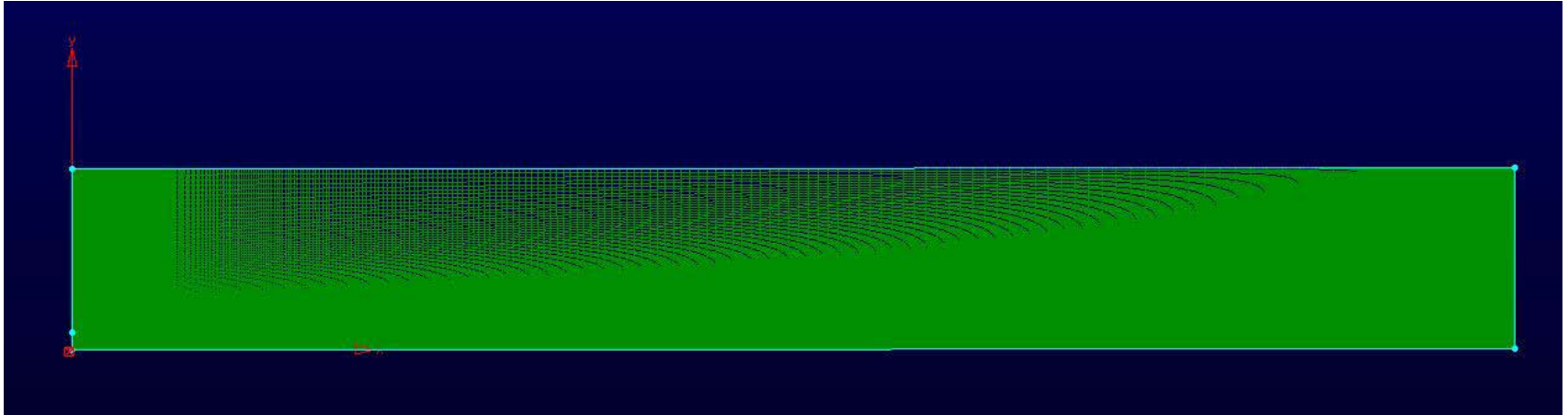
## Droplet Inlet Boundary Condition (1D downstream)

Variable	Constants
Excess axial mean velocity (m/s) $U_e = U_{eo} [1 - [\sin((R/R_{1/2U})^{n_2})]^{n_1}]$	(1) Peak excess axial mean velocity, $U_{eo}$ $U_{eo} = -0.05148 d + 21.97494$ where $d$ is droplet diameter ( $\mu\text{m}$ ) (2) $n_1 = 3.9320$ , $n_2 = 1.222$ , $R_{1/2U} = 4.978$
Radial mean velocity (m/s) $V = 0$	
Volume fraction $r = r_o \exp[-A(R/R_{1/2VF})^n]$	(1) Peak volume fraction $r_o$ 4.32E-08 (5 $\mu\text{m}$ ), 6.91E-07 (15 $\mu\text{m}$ ), 5.07E-06 (25 $\mu\text{m}$ ), 9.50E-06 (35 $\mu\text{m}$ ), 1.47E-05 (45 $\mu\text{m}$ ), 2.16E-05 (55 $\mu\text{m}$ ), 2.04E-05 (65 $\mu\text{m}$ ), 7.43E-06 (75 $\mu\text{m}$ ), 2.50E-06 (85 $\mu\text{m}$ ) (2) $A = 0.6942$ , $n = 2.1543$ , $R_{1/2VF} = 3.9480$
Gas turbulent kinetic energy ( $\text{m}^2/\text{s}^2$ ) $k = D \exp[-A(R - B)^n] + C$	(1) $A = 1.011$ , $B = 4.904$ , $C = 1.75$ , $D = 8.73$ , $n = 1.418$
Gas turbulent energy dissipation ( $\text{m}^2/\text{s}^3$ ) $\varepsilon = \frac{k^{1.5}}{0.2D}$	(1) $D = 0.0098 \text{ m}$

Nijdam, J., Langrish, T., & Fletcher, D. (2008). Assessment of an Eulerian CFD model for prediction of dilute droplet dispersion in a turbulent jet. *Appl. Math. Model.*, 2686-2705.



# Model Validation Case



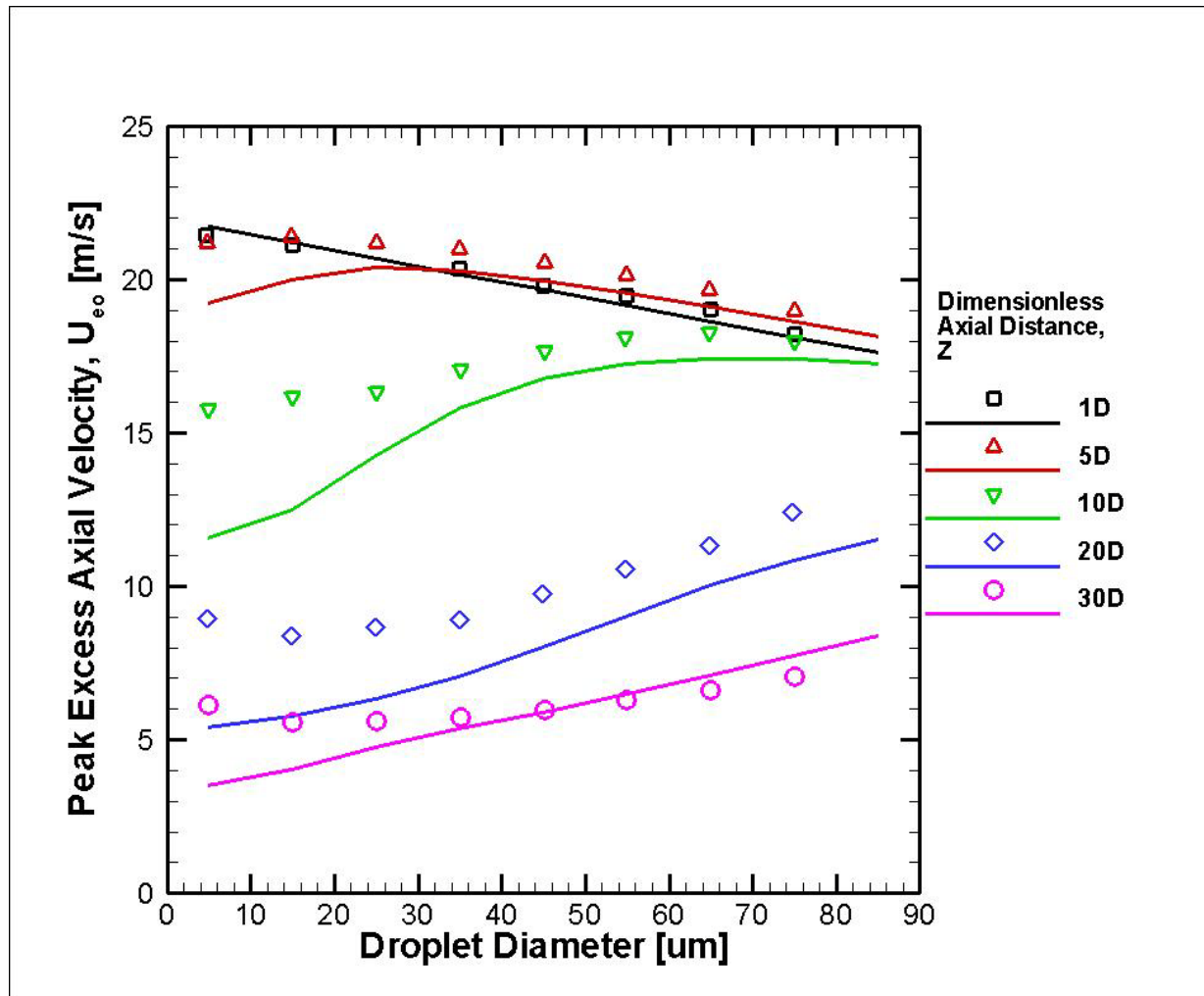
## Case Conditions:

- Two species (Air, Turpentine)
- Base Equation Type: Compressible Real Gas Navier-Stokes/Euler
- Equation of State: Ideal Gas
- Turbulence Simulation: RANS, realizable k-eps or SST
- Turbulence Intensity: 1.4%
- 10 um droplet size bins from 5-85 um diameter
- Temperature-based inlet profiles generated with Matlab script

- 79000 quadrilateral cells
- Total domain size = 0.05 m x 0.4 m

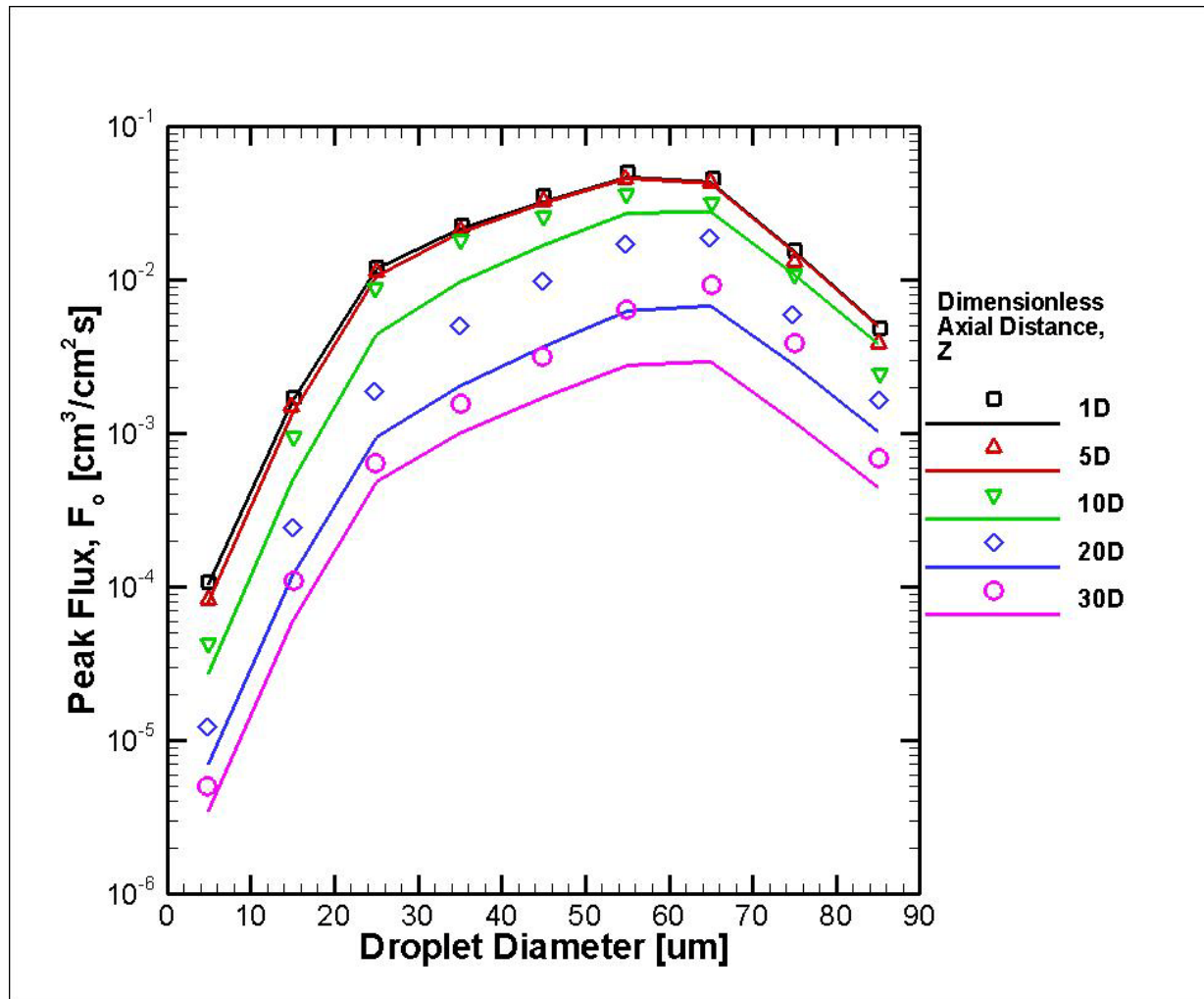


# Results





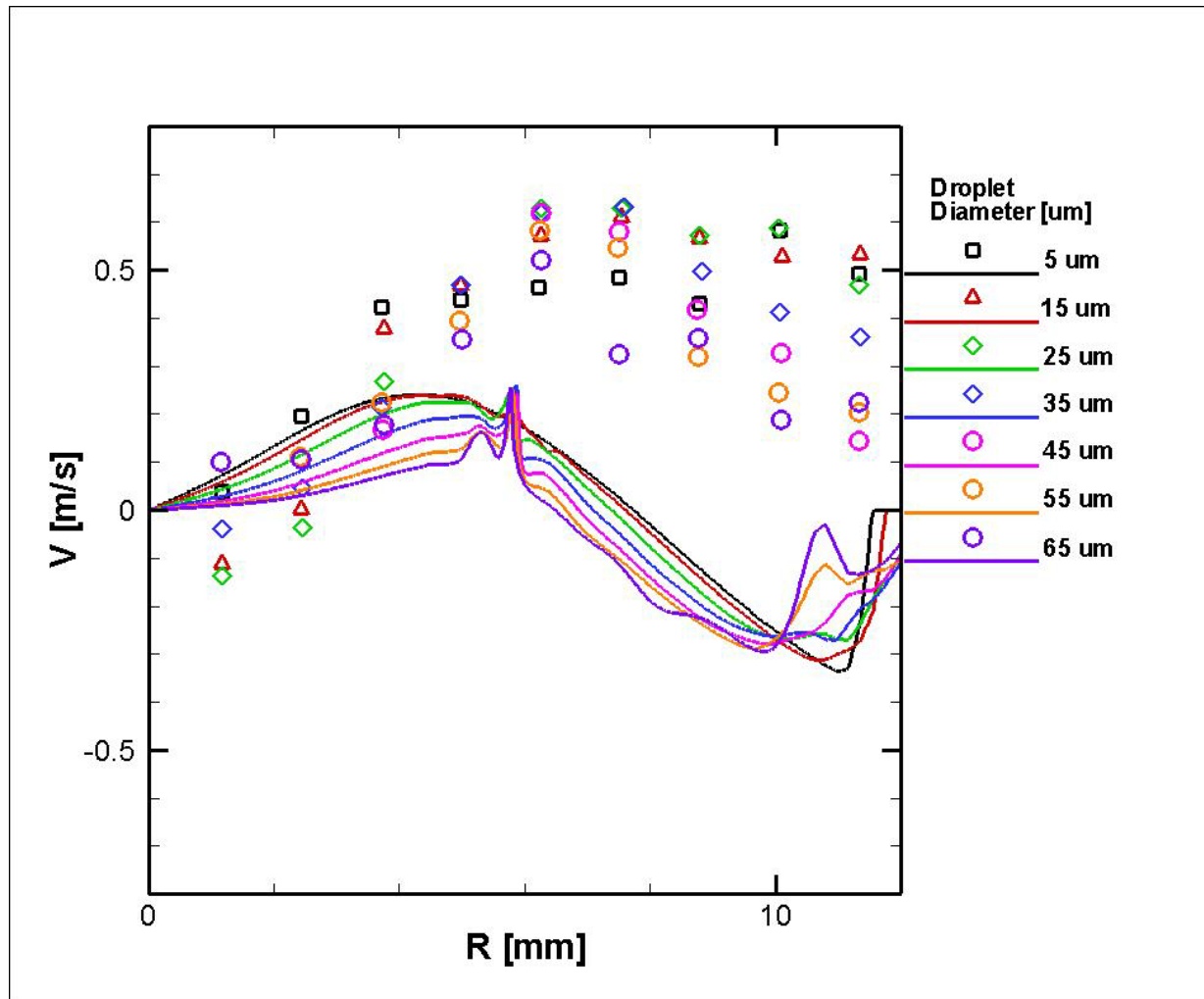
# Results







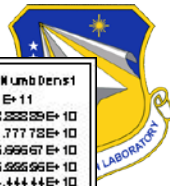
# Results





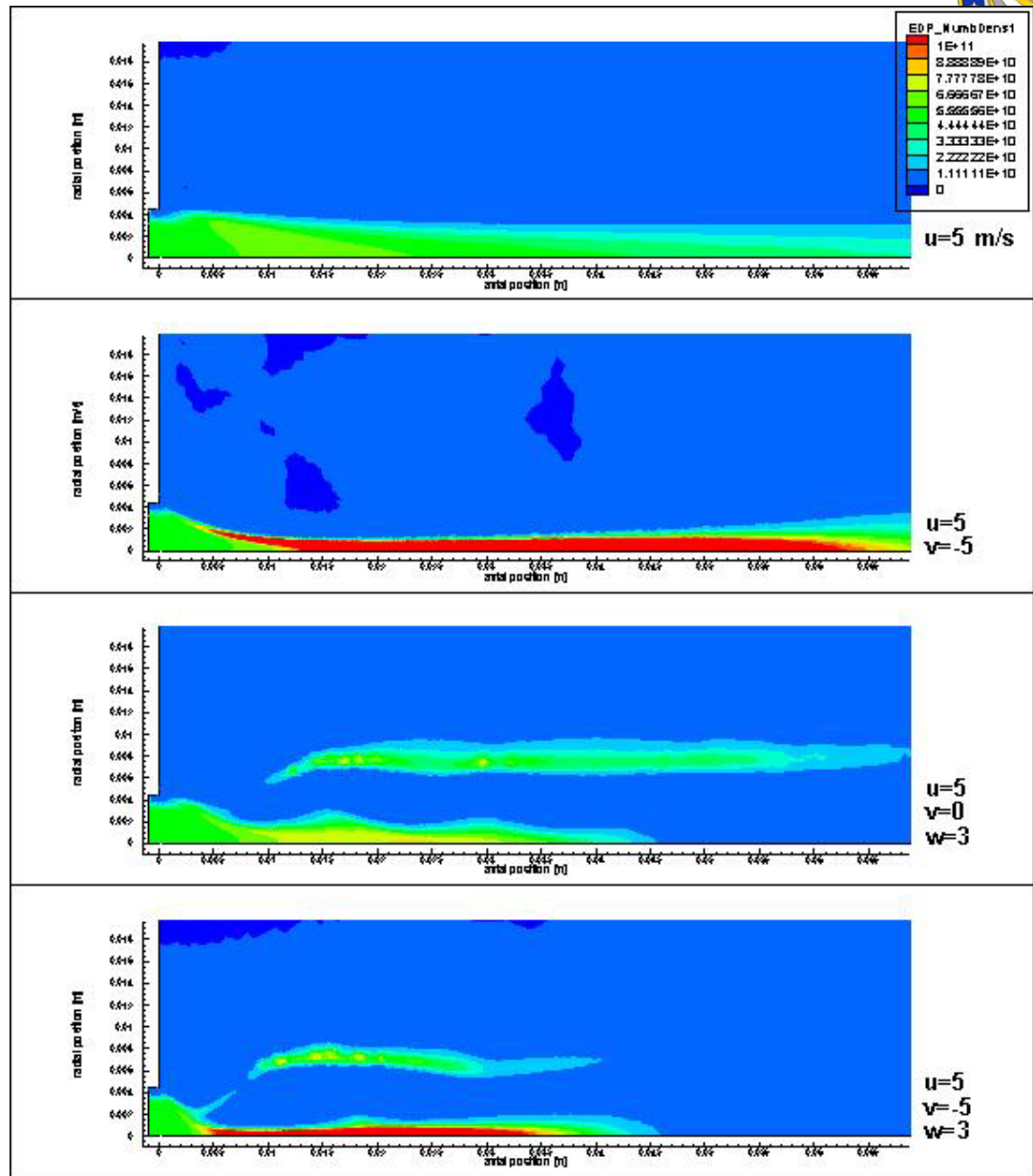
# Summary

- Excess axial velocities of smaller droplets up to 50% slower than experimental while larger droplets show better agreement
- Error for peak volumetric fluxes higher for larger droplets—may be due to the fact that they carry more volume
- CFD agreement with radial velocities is poor— may be measurement error
- EDP features available in CFD++ may be missing important physics



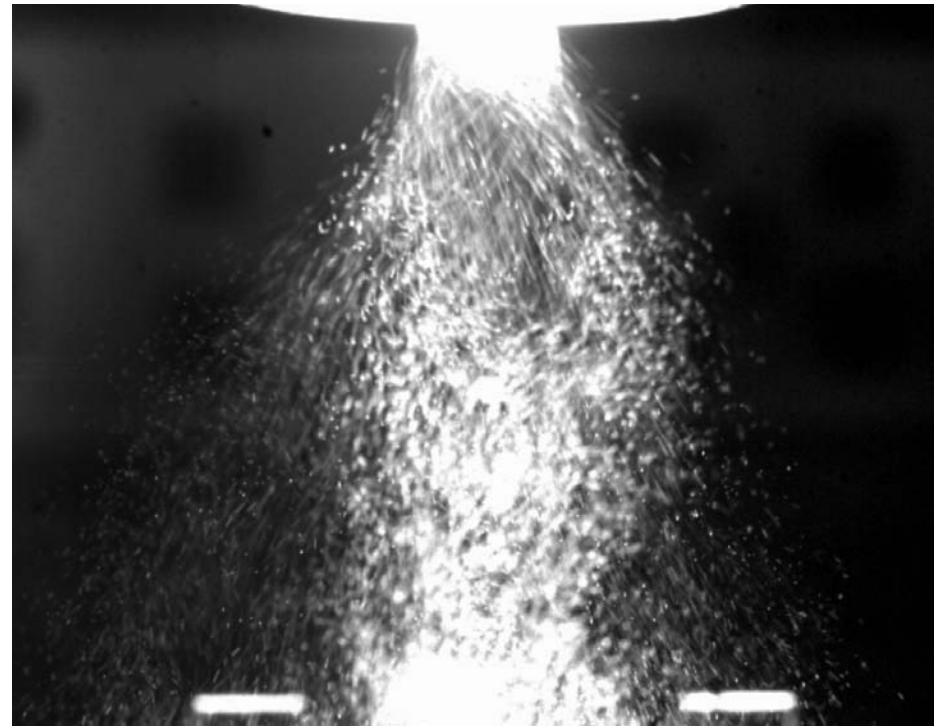
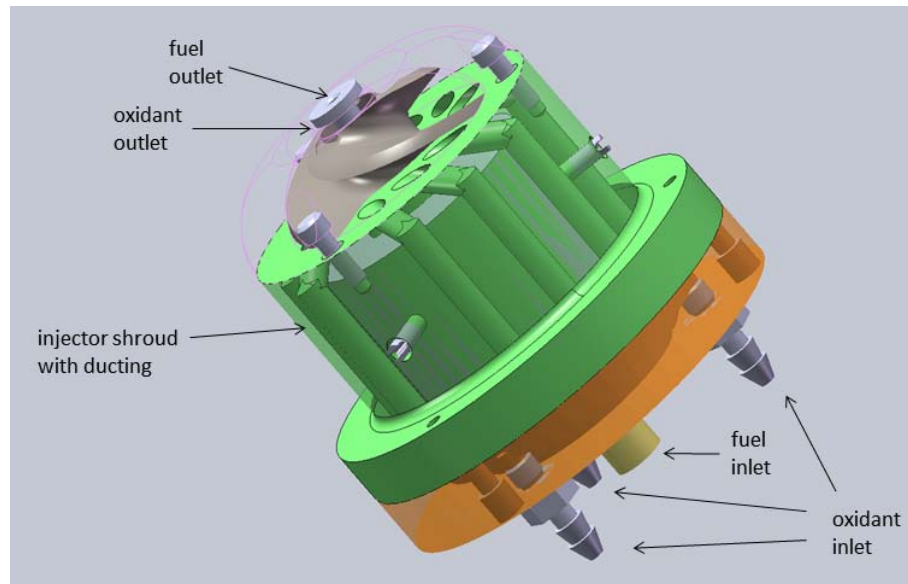
## Future Work

Parametric study of effects of co-flow velocity components on droplet mixing





# Future Work



Use CFD to design and determine conditions for experimental setup for testing combustion ignition strategies



# Questions?

